

# A High- $Q$ Terahertz Resonator for the Measurement of Electronic Properties of Conductors and Low-Loss Dielectrics

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**Abstract**—The successful engineering of sources and components in the terahertz (THz) regime benefits from good characterization of materials properties. Previous research reports have shown that calculations of material parameters that are valid at radio frequencies are no longer accurate at THz frequencies. A high-quality-factor quasi-optical hemispherical resonator operating between 300 GHz–1 THz has been designed and implemented for the measurement of electronic properties of conductors as well as low-loss dielectrics. This apparatus is the first quasi-optical resonator to achieve  $Q \approx 4 \times 10^5$  at frequencies greater than 400 GHz in the THz regime. It is also the first open resonator designed to measure effective conductivity at these frequencies. This paper discusses the techniques that enabled high- $Q$  operation in the THz regime. It also includes measurements of silicon with different doping densities and conductors of various surface roughness values with comparison to theoretical predictions.

**Index Terms**—Conductivity, resonator, roughness, terahertz.

## I. INTRODUCTION

THE utilization of the terahertz (THz) or submillimeter regime of the electromagnetic spectrum is hindered by a lack of effective and convenient sources and amplifiers. Among the challenges to building these devices is the need for a validated physical model for the electronic properties of materials involved in THz system design [1]. The most fundamental materials property for many components is the

complex permittivity, which consists of the relative permittivity (or refractive index) and the conductivity (or the loss tangent). These materials parameters relate directly to both the losses in a device and the functionality of a component. They are crucial in the design of next-generation sources and amplifiers, especially for vacuum electronics [2]. The relative permittivity values of most materials in the THz regime are close to their static values [3]. The conductivity, or loss tangent, proves to be more challenging to measure and predict.

While it is common knowledge that effective surface resistivity of metals is higher in the THz regime than at RF frequencies, scientists have not sufficiently characterized the relationship between THz surface resistivity, frequency, and surface characteristics to provide practical predictive capabilities [4]–[6]. While there has been good progress towards the modeling of the intrinsic surface resistivity of bulk metals [7]–[9], the exact relationship between surface roughness and effective conductivity is still unquantified. Such information is critical to the development of next-generation sources and detectors. The current microfabrication techniques used to create up-and-coming vacuum electronics devices have sidewall roughness features on the order of 50 nm, which is close to the skin depth of gold at 650 GHz [10]–[14]. Successfully characterizing the above relationships requires a means to empirically measure effective conductivity beyond 400 GHz. Such an apparatus has not been demonstrated prior to this paper.

In this paper, we demonstrate the feasibility of building a resonator at frequencies beyond 400 GHz with a sufficiently high quality factor for sensitive measurements of dielectrics and conductors. The presented apparatus is the first of its kind to measure effective conductivity over a small area at these frequencies while providing a framework to easily exchange and compare two samples. The measurement area of less than 13 mm<sup>2</sup> provides the unique capability to determine the conductivity of controlled submicron roughness topographies that are difficult to fabricate over large areas. This measurement area can be further decreased if the resulting larger expansion angle of the Gaussian beam is acceptable, e.g. by fabricating larger mirrors or shortening the distance between elements to minimize diffraction losses. The above features enable further ongoing research aimed at characterizing the relationship between surface roughness—including roughness resulting from nanofabricated features—and conductivity in the THz regime.

We also discuss the solutions developed to overcome the unique challenges of operating at such frequencies. The techniques presented include using a single coupling film and wire

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grids to overcome the low ratio between the THz source power and detector sensitivity, characterizing non-negligible coupling film loss, improvements on a previously published curve-fitting technique, and an analysis of remaining sources of system error. Examples of the resonator's application are also described at 400 and 650 GHz.

In Section II, we provide a background of previous work on measuring electronic materials properties using open resonators and provide details on the design and implementation of the apparatus in this paper. In Section III, we report electrical properties of dielectrics such as silicon using the resonator system. The resonator was also used to measure conductors and the results are described in Section IV. In Section V, we summarize the results and discuss their implications.

## II. CURRENT STATE OF THE ART AND THE PROPOSED METHOD

### A. Existing Approaches to Measuring THz Electronic Properties

Scientists and engineers have used open resonators to measure the electronic properties of materials since the 1960s [15]. Resonance peaks can be found by recording the return power while varying the frequency of the input signal that is being coupled into the resonator. The sharpness, or quality factor ( $Q$ ), of the peaks correlates to the losses within the resonator, including the reflection and absorption losses of the device under test. The resonance frequencies relate to the optical path length of the resonator, which changes when the device under test is inserted.

The operating frequency of these resonators has progressively increased over the years, as new radiation sources have become available [16]–[18]. As the frequency increases past the  $W$ -band, many traditional microwave approaches become impractical. Waveguide and coaxial propagation become lossy, resulting in the need for free-space quasi-optical techniques [19], [20]. The precision required for successful iris coupling also becomes increasingly difficult beyond 100 GHz, which necessitates alternative coupling approaches such as the use of a thin coupling film. Implementing the above changes has enabled measurements via the resonator approach of dielectric constant, loss tangent, and conductivity values at frequencies beyond the  $W$ -band up to 380 GHz [19]–[21].

Time-domain spectroscopy (TDS) has been the primary approach to obtaining measurements beyond 200 GHz [22]–[24]. This technique, however, is mainly limited to low-loss samples. While reflective TDS has been demonstrated, it is difficult and very sensitive to positioning errors [25]. Time-domain spectroscopy ellipsometry (TDSE) combines TDS with ellipsometry to overcome much of the sensitivity to positioning errors but still requires a large angle of incidence to the sample due to the nature of the design [26]. The TDSE technique is being continually refined and was successfully applied to characterize thin dielectric films [27]. The resonator technique presented in this paper complements existing TDS and TDSE technology by providing the ability to perform measurements of samples at a normal incident angle. It is well-equipped to measure high-loss samples and conductors. High-loss samples can be fabricated as thin films for higher transmission and placed on the surface of one of the mirrors for structural support. Good conductors can be characterized by substituting one of the resonator mirrors for

the material being measured. The combined capabilities of this resonator technique and TDSE allow the measurement of effective conductivity at a variety of angles of incidence. This ability is necessary for in-depth studies of reflection losses due to surface features that may have an angular dependence.

Building a resonator at THz-regime frequencies above 400 GHz has a unique set of challenges that do not exist below 100 GHz. The effective optical thickness of the coupling films is more than four times larger. This makes the films more reflective, causing them to couple more energy out of the resonator, which in turn lowers the quality factor and sensitivity. Using an increasingly thinner film becomes problematic because it lowers the power of the return signal. The ratio between the source power and detector sensitivity is much lower at these frequencies, primarily due to the low power of available radiation sources. Therefore, the design parameters of the resonator must fall in a narrow window where the quality factor is sufficiently high while still returning sufficient power to the detector. This restriction typically means that, unlike previous resonators, the coupling film is thick enough to have a non-negligible loss that must be taken into account when evaluating  $Q$ .

### B. Overview of Proposed Method

Fig. 1 gives an overview of the resonator system described in this paper. The THz source consists of a microwave frequency synthesizer connected to an amplifier multiplier chain (AMC). The AMC up-converts the signal from the synthesizer by a large factor into the THz regime. For the examples described in this paper, two AMCs up-converts the synthesizer signal by factors of 36 or 48 to produce a frequency at 400 or 650 GHz, respectively, and an operating bandwidth of 4 GHz. The signal is polarized horizontally such that it passes through the vertical wire grid. The two focusing mirrors reshape the beam for optimal coupling into the resonator. Due to the 45-deg wire grid, the polarization of the signal coupled into the resonator is at a 45-deg angle compared to the initial output of the AMC.

As the THz signal travels between the two resonator mirrors, a fraction of the power is reflected back out into the elliptical focusing mirrors and through the 45-deg wire grid. The vertical wire grid separates the return signal from the input signal and sends half of the return signal to the Goly cell. The sensitivity of the Goly cell is enhanced by a lock-in amplifier, allowing it to detect signals below 100 nW.

The variation of the input frequency,  $\nu$ , over the range of the AMC allows identification of periodic cavity resonance peaks in the return signal at the Goly cell detector. The distance between peaks,  $\Delta\nu$ , is equal to  $c/(2L)$ , where  $c$  is the speed of light and  $L$  is the resonator length (the distance between the two mirrors). This relationship provides an initial assessment of the resonator length.

$P(\nu)$  is found by curve-fitting a Lorentzian function to the data points [28]

$$P(\nu) = \frac{C_1}{\pi C_2 \left[ 1 + \left( \frac{\nu - C_3}{C_2} \right)^2 \right]} + C_4 \quad (1)$$

where  $P(\nu)$  is the measured return power, and  $C_1$ ,  $C_2$ ,  $C_3$ , and  $C_4$  are curve-fit parameters.  $C_2$  represents the half-width-at-half-maximum (HWHM), or one-half of the full-width-at-half-

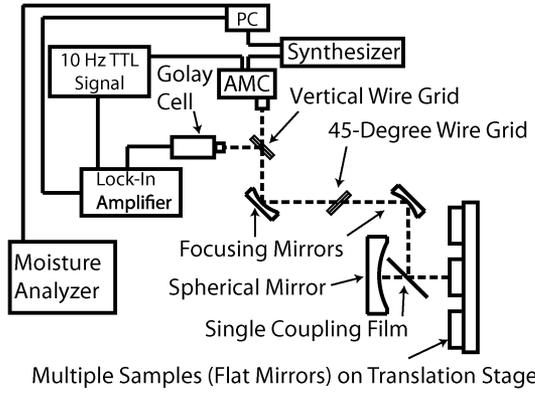


Fig. 1. Schematic of the resonator system. The AMC emits THz radiation that is reshaped by the focusing mirrors and coupled into the resonator through a single coupling film. The resonator consists of two mirrors: the diamond-turned copper mirror and the device under test, which serves as a flat mirror. While the signal travels between the two mirrors, the coupling film reflects a fraction of it back through the focusing mirrors. A series of wire grids placed along the return path directs a portion of the return signal to the Golay cell, whose sensitivity is enhanced by the lock-in amplifier. The moisture analyzer monitors the humidity to ensure that atmospheric propagation losses are successfully minimized by the desiccants and sealed enclosure surrounding the apparatus.

maximum (FWHM) of the peak.  $C_3$  is equal to the center frequency,  $\nu_C$ .  $C_4$  corresponds to the broadband noise.  $C_1$  is related to the peak power at the resonant frequency,  $P_{\max}$ , by  $C_1 = \pi C_2(P_{\max} - C_4)$ .

There has been a previous report of an iterative approach producing good three-parameter curve fits to the equation above—without the  $C_4$  term—when the signal-to-noise ratio is low [29]. Additional experimentation revealed that a similar effect can be found by adding in a fourth parameter,  $C_4$ , to represent the broadband noise. We found the four-parameter curve fit to be more efficient and robust than an iterative, three-parameter curve fit. Once the curve fit is complete, the key characteristics needed to determine relative permittivity and effective conductivity can be extracted from the curve fit parameters:

$$\nu_c = C_3 \quad (\text{center frequency}) \quad (2a)$$

$$Q = \frac{\nu_c}{\nu_{\text{FWHM}}} = \frac{C_3}{2C_2} \quad (\text{quality factor}) \quad (2b)$$

where  $\nu_{\text{FWHM}}$  represents the FWHM.

Multiple measurements and curve fits are performed for the data in this study, and the standard deviation of each measurement is tracked and logged. The measured quality factor,  $Q_{\text{tot}}$ , is related to the individual sources of loss in the resonator by the following relationship:

$$\frac{1}{Q_{\text{tot}}} = \sum_{i=1}^n \frac{1}{Q_i} = \frac{c}{2\pi\nu_c L} \sum_{i=1}^n \kappa_i \quad (3)$$

where  $\kappa_i$  is the fractional loss that the signal experiences during a one-way trip. Fig. 2 visually summarizes the various sources of loss considered during the design of the resonator system: losses due to diffraction ( $\kappa_D$ ), misalignment ( $\kappa_L$ ), atmospheric scattering and absorption ( $\kappa_A$ ), the coupling film ( $\kappa_C$ ), and reflection losses due to the surface impedance of the two mirrors ( $\kappa_{R1}$  and  $\kappa_{R2}$ ).

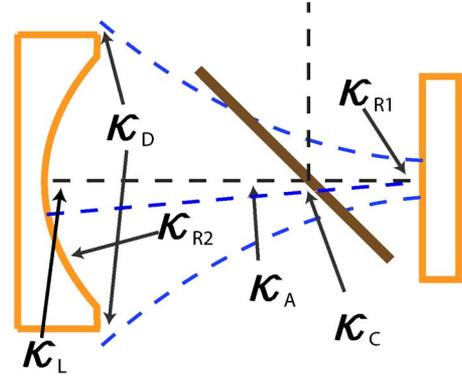


Fig. 2. Definition of various sources of losses within the resonator.

In order to have maximum sensitivity to changes in one-way loss when a sample is incorporated in the resonator, all sources of loss must be made as small as possible relative to the reflection losses of the mirror ( $\kappa_{R1}$  and  $\kappa_{R2}$ ). The losses due to diffraction have been made negligible in the design phase by ensuring that the diameter of both mirrors exceed four times the  $1/e$  radius, resulting in a one-way trip loss of two orders of magnitude smaller than  $\kappa_{R1}$  and  $\kappa_{R2}$ . The loss due to misalignment has also been minimized through the addition of alignment pins on almost all of the components. The remaining parts that cannot incorporate alignment pins have optical mirrors mounted on key surfaces, allowing alignment with the aid of a visible laser. The resulting angular misalignment in the resonator system is less than 2 mrad, making  $\kappa_L$  much smaller than  $\kappa_{R1}$  and  $\kappa_{R2}$ .

Water content is the primary source of atmospheric loss ( $\kappa_A$ ). In order to minimize water-content, a hermetically-sealed enclosure was built around the system with electrical feed-through ports and moisture analyzers. The inclusion of molecular sieve desiccant brings the water content in the enclosure down to between 50–100 parts-per-million by volume (ppmV). Measurements and model predictions [30] demonstrate propagation losses within this range are insignificant compared to the remaining sources of loss.

As mentioned previously in this paper, successful operation at 400 GHz and above requires a balance between a high quality factor and strong return signal. One of the initial challenges was the thick coupling film required to produce a detectable return signal. Initial calculations found that the separate input and output coupling films used in *W*-band resonators [19] would raise the coupling loss,  $\kappa_C$ , and lower the quality factor beyond the required value for sensitive conductivity measurements. This is because at 650 GHz, the coupling films are optically thicker to the THz signal than a *W*-band one, resulting in a higher  $\kappa_C$ . The resonator design overcame this challenge by having a single 5- $\mu\text{m}$  polytetrafluoroethylene (PTFE) film serve as both the input and output coupling films, which halves the coupling film loss. The vertical and 45-degrwire grids direct a portion of the return signal towards the Golay cell detector at the cost of a 75% round-trip loss.

Unfortunately, even with these improvements, the 5- $\mu\text{m}$  PTFE film still results in a non-negligible  $\kappa_C$  when compared to  $\kappa_{R1}$  and  $\kappa_{R2}$ . Unlike resonators operating at lower frequencies, where the solution is to use ever-thinner films at the cost of a weaker return signal, the current system is prohibited from

doing so due to the low output power ( $<1$  mW) available at 400 and 650 GHz. As such, characterization of  $\kappa_C$  is necessary.

Experimental measurements validated initial theoretical estimates of  $\kappa_C$ ,  $\kappa_{R1}$  and  $\kappa_{R2}$ . First, care was taken such that the planar and spherical mirrors were manufactured from the same slab of bulk oxygen-free copper using the same diamond-turning technology so that they had similar surface features and chemical compositions. Both diamond-turned copper mirrors were characterized using an interferometer to have an RMS roughness of less than 6 nm—less than 1/10 of the skin depth of copper at 650 GHz—ensuring minimal reflection losses compared to any device under test that is subsequently inserted. These efforts ensured that both mirrors have a similar effective conductivity, and thus

$$\kappa_{R1} \approx \kappa_{R2} = \kappa_R^{Cu}. \quad (4)$$

By treating the thin coupling films as a dielectric slab with material properties from published measurements [3] and taking into account multiple reflections, the ratio of the coupling loss between a 5- $\mu\text{m}$  and 10- $\mu\text{m}$  PTFE film was established ( $\kappa_C = \kappa_C^5$  or  $\kappa_C^{10}$ ) [31]

$$\kappa_C^{10} = M\kappa_C^5, \quad (5)$$

where

$$M = 3.97 \quad \text{at 400 GHz} \quad (6a)$$

$$M = 3.93 \quad \text{at 650 GHz.} \quad (6b)$$

The quality factor using both coupling film thicknesses ( $Q_m^5$  for the 5  $\mu\text{m}$ -thick film and  $Q_m^{10}$  for 10  $\mu\text{m}$ -thick film) were measured at both 400 and 650 GHz. Given that  $\kappa_{R1} \approx \kappa_{R2} = \kappa_R^{Cu}$  and  $\kappa_D, \kappa_L, \kappa_A \ll \kappa_C, \kappa_R^{Cu}$ , (3), (5), (6a) and (6b) can be rewritten to provide a system of two equations and two unknowns for each frequency

$$\kappa_R^{Cu} + \kappa_C^5 = \frac{2\pi\nu L}{cQ_m^5} \quad (7)$$

$$\kappa_R^{Cu} + M\kappa_C^5 = \frac{2\pi\nu L}{cQ_m^{10}}. \quad (8)$$

Solving this system of two equations provides a value for both the coupling loss of the 5- $\mu\text{m}$  film as well as the effective conductivity of the diamond-turned mirrors. Measurements of  $Q_m^5$  and  $Q_m^{10}$  resulted in  $\kappa_C^5$  and  $\kappa_C^{10}$  that were within 5% of the expected calculated thin-film values using published dielectric constants [3], [31]. This information enabled the measurement of absolute, instead of relative, effective conductivity values of metal samples using a process described in Section IV.

With  $\kappa_C$ ,  $\kappa_{R1}$ , and  $\kappa_{R2}$  characterized and all other sources of loss made negligible, (3) can be written as

$$\frac{1}{Q_{\text{tot}}} = \frac{c}{2\pi\nu L} \left[ \kappa_C + \frac{1}{2}(\kappa_{R1} + \kappa_{R2}) \right]. \quad (9)$$

The resonator can then be used to measure properties of low-loss dielectrics or semiconductors and metals by inserting the sample as depicted in Fig. 3. The information can then be extracted from a comparison with the unloaded case, where the diamond-turned spherical and flat mirrors are used. The sample with the highest loss loaded into the resonator that still provided

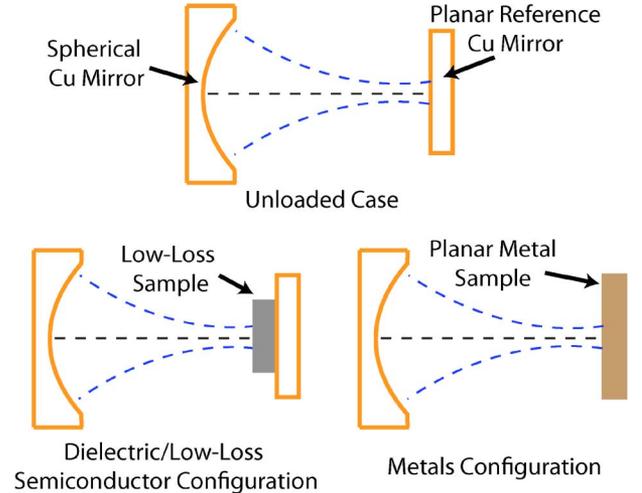


Fig. 3. Various configurations of the resonator.

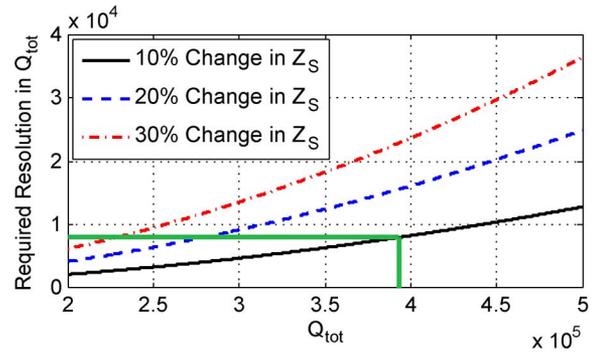


Fig. 4. The calculated quality factor resolution necessary in order to detect a 10%, 20% and 30% change in the surface resistance,  $Z_S$ , as a function of the unloaded quality factor,  $Q_{\text{tot}}$ . The plot shows that the existing  $Q$  of  $3.9 \times 10^5$  and resolution of approximately  $10^4$  is sufficient to detect a roughly 10% change in surface resistance.

a detectable return signal produced a  $Q$  corresponding to a 4.7% one-way fractional power loss. This result provides an approximate upper limit to the amount of acceptable loss for a dielectric sample or reflecting conductor before necessitating further pre-measurement processing, such as applying a thicker coupling film at the expense of lower  $Q$  and sensitivity or thinning the dielectric sample.

The resolution in measured effective conductivity depends mostly on the resolution of the measured  $Q$ . The characterization process of the resonator found a nominal unloaded  $Q = 3.9 \times 10^5$  with a repeatability of just under  $1 \times 10^4$ . Fig. 4 shows the change in  $Q_{\text{tot}}$  in (9) when the flat mirror's surface impedance,  $\kappa_{R1}$ , changes by 10%, 20%, and 30%. The  $Q$  resolution is sufficient to detect an approximately 10% change in the surface impedance of the sample. The sensitivity increases if the sample has a conductivity much lower than the diamond-turned copper mirror, since it becomes the dominating  $\kappa_i$  in (3).

The specified fabrication tolerances, such as deviation in curvature of the spherical mirror and distance to the planar mirror, have negligible effects on the radiation power, relative frequency shift, and quality factor of the resonance curves. The measured resonator loss matches the expected value due to

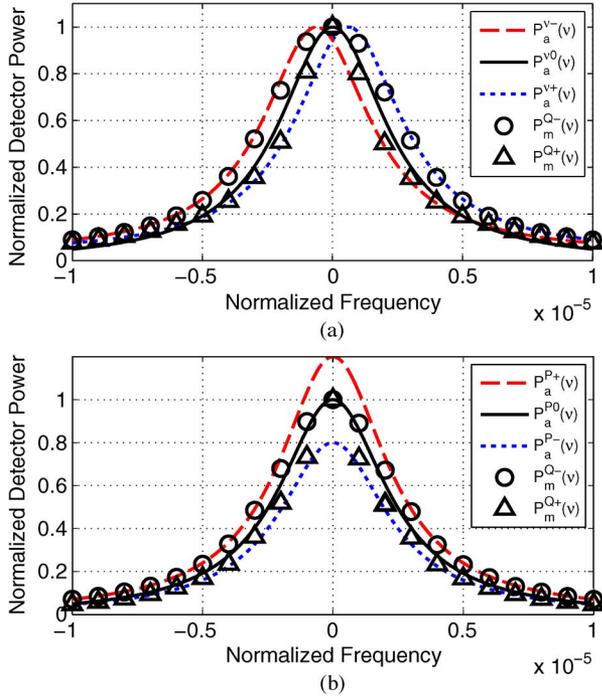


Fig. 5. Variation in measured quality factor due to two potential causes: (a) shifts in the center frequency from  $P_a^{\nu-}(\nu)$  to  $P_a^{\nu+}(\nu)$  caused by a change in resonator length during the resonance scan can cause an error in the inferred  $Q$ ; (b) changes in the power of the radiation source during a resonance scan from  $P_a^{P0}(\nu)$  to either  $P_a^{P+}(\nu)$  or  $P_a^{P-}(\nu)$  can cause an error in the inferred  $Q$ . In both (a) and (b), the circles of  $P_m^{Q-}(\nu)$  illustrate a case where the apparent measured line width is broader than the actual one, resulting in a lower  $Q$ . The triangles of  $P_m^{Q+}(\nu)$  illustrate a case where the measured line width is narrower the actual one, resulting in a higher  $Q$ .

mirror reflection and coupling film loss alone. This correlation shows that primary contributors to the measured  $Q$  are the reflection and coupling film loss, not fabrication errors.

A sensitivity analysis shows that the above fabrication errors can change the  $Q$  by  $\approx 1/10$  of the measured repeatability of  $1 \times 10^4$ . Therefore, a closer look at other causes of the observed repeatability is warranted. Assuming that the losses in the resonator are steady during the resonance peak measurement, the other principle candidate sources of the  $1 \times 10^4$  observed variation in  $Q$  are instabilities in either the resonator length or AMC signal strength. The following two subsections provide a quantitative exploration to establish these two factors as reasonable causes of the observed uncertainty.

### C. Sources of Uncertainty: Resonator Length

A change in resonator length during data acquisition alters the center frequency of the peak, which can cause the measured peak to become broader or narrower than the actual one. Fig. 5(a) illustrates this concept. The various lines represent Lorentzian curves with the same quality factor but different center frequencies. Depending on whether the frequency is shifting to the left or the right during measurement, the observed quality factor can be lower (circular data points in the figure) or higher (triangular data points) than the actual value.

An estimation of the change in resonator length that results in the observed uncertainty can be derived by examining the

Lorentzian in (1). Since the signal-to-noise ratio of typical measurements is approximately 10:1, we focus on the broadening at the point where the power has dropped to 1/10 of its maximum value, or the full-width-at-1/10-maximum points. By setting  $P(\nu) = P_{\max}/10$  and solving for the frequency,  $\nu$ , it can be found that this power occurs at a frequency ( $3 \times \text{HWHM}$ ) from the center frequency.

To model the broadening, suppose that the system has an actual frequency response of  $P_a(\nu)$ , with a quality factor of  $Q_a$  and HWHM of  $\text{HWHM}_a$ . During measurement, the center frequency shifts from  $\nu_c$  to  $\nu_s = \nu_c + \delta\nu$ , resulting in an observed frequency response of  $P_m^{Q-}(\nu)$ . This measured  $P_m^{Q-}(\nu)$  has an erroneously lower  $Q$  of  $Q_m$  and HWHM of  $\text{HWHM}_m$  compared to the actual value. The transition from the  $P_a^{\nu-}(\nu)$  curve to the  $P_a^{\nu+}(\nu)$  curve in Fig. 5(a) represent the actual frequency response,  $P_a(\nu)$ , with frequency shifts during measurement. The circles of  $P_m^{Q-}(\nu)$  in Fig. 5(a) represent the measured frequency response that is erroneously broadened. This shift in the center frequency can result from a resonator length shift of  $\delta L$  during measurement:

$$\delta L = \frac{c}{2} \left( \frac{1}{\nu_c} - \frac{1}{\nu_s} \right). \quad (10)$$

As the Lorentzian fit incorporates all data points above the noise level (between full-width-at-1/10-maximum points), it can be shown that the measured  $\text{HWHM}_m$  will be larger than the actual  $\text{HWHM}_a$  by:

$$\text{HWHM}_m = \text{HWHM}_a + \frac{\delta\nu}{3} \quad (11)$$

resulting in a  $Q_m$  that can be compared with the actual quality factor,  $Q_a$ , using (2b)

$$Q_a = \frac{\nu_c}{2\text{HWHM}_a} \quad (12)$$

$$Q_m = \frac{\nu_c + \left(\frac{1}{2}\right)\delta\nu}{2\text{HWHM}_a + \left(\frac{2}{3}\right)\delta\nu}. \quad (13)$$

Comparing the numerators and denominators confirms that  $Q_m$  is indeed smaller than  $Q_a$ . A similar analysis with a change in algebraic signs applies to the case where the center frequency shifts to a smaller value during measurement ( $\nu_s = \nu_c - \delta\nu$ ) yielding an erroneously smaller value of  $\text{HWHM}_m$  and thus a higher  $Q_m$ . This scenario is illustrated by the triangular data points of  $P_m^{Q+}(\nu)$  in Fig. 5(a).

The above equations suggest that a change in resonator length on the order of 110 nm is sufficient to result in the observed  $Q$  uncertainty of  $1 \times 10^4$ . The resonator is mounted onto a standard optical table that is primarily made of stainless steel. Using a typical thermal expansion coefficient for stainless steel of  $10.4 \mu\text{m}/^\circ\text{C}$  [32], the temperature change required for a resonator length drift of 110 nm is a mere  $0.011^\circ\text{C}$ .

Each measurement of a resonant peak takes between 30 min to 1 h, depending on the measurement parameters. The temperature in the room housing the experiment is not tightly controlled and the ambient temperature can change as much as  $1^\circ\text{C}$  over the course of a series of measurements. Therefore, it is reasonable to suggest that the core temperature of the table could drift

by the 0.011 °C necessary to create the observed uncertainty in  $Q$  during a single resonance scan.

#### D. Sources of Uncertainty: AMC Power

Power fluctuations in the AMC signal source can also result in a measured  $Q$  that is higher or lower than the actual value. Fig. 5(b) illustrates this concept by plotting multiple Lorentzian curves of identical quality factors but differing maximums. Again, taking measurements as the system varies between the different power levels can result in measured  $Q$ s that are lower (circular data points of  $P_m^{Q-}(\nu)$  in the figure) or higher (triangle data points of  $P_m^{Q+}(\nu)$ ) than the actual value.

First, we define two curves:  $P_a^{P0}(\nu)$ , illustrated in Fig. 5(b), corresponds to the actual frequency response of the system and takes the form of (1), where  $C_2 = \text{HWHM}_a$ , or the actual HWHM. It has a quality factor of  $Q_a$ , which is related to  $C_2$  by (2b). We also define  $P_m^{Q-}(\nu)$ , which corresponds to a measured frequency response that has an erroneously lower quality factor,  $Q_m < Q_a$ , and is represented by the circles in Fig. 5(b). Its HWHM,  $\text{HWHM}_m$ , is also related to  $C_2$  by (2b). Both curves have peaks centered at  $\nu_c$ .

We set  $Q_a = 3.9 \times 10^5$ , which is the nominal, unloaded  $Q$  of the system. Since the observed repeatability is  $1 \times 10^4$ , we let  $Q_m$  represent a worst-case measurement at the limits of the observed uncertainty, or  $Q_m = 3.85 \times 10^5$ . These values, along with the information in the previous paragraph, gives the parameters to define  $P_a^{P0}(\nu)$  and  $P_m^{Q-}(\nu)$ .

To correlate with the observed signal-to-noise ratio, emphasis is again placed at the full-width-at-1/10-maximum points, or  $3 \times \text{HWHM}$  from the center frequency. The power fluctuation that would result in the observed uncertainty can be calculated by finding the fractional power difference,  $\delta P/P$ , at the point of interest

$$\frac{\delta P}{P} = \frac{P_m^{Q-}(\nu_c - 3 \times \text{HWHM}_m) - P_a^{P0}(\nu_c - 3 \times \text{HWHM}_a)}{P_a^{P0}(\nu_c - 3 \times \text{HWHM}_a)}. \quad (14)$$

Evaluating (14) with the above values shows that a power drift on the order of  $\delta P/P \approx 2\%$  is sufficient to result in the observed  $1 \times 10^4$  variation in  $Q$ . A similar analysis leading to the same result can be performed with  $Q_m = 3.95 \times 10^5$ , which corresponds to power fluctuations resulting in an erroneously higher  $Q$ , as illustrated by the triangular points of  $P_m^{Q+}$  in Fig. 5(b). In order to minimize the effects of environmental variations and obtain several measurements in a reasonable length of time, it is necessary to step the frequency every 10–20 s. The AMC potentially has not had sufficient time to thermally stabilize during this time. Therefore, it is reasonable to hypothesize that the AMC output power is varying by the 2% necessary to cause the observed variation in measured  $Q$ .

### III. MEASUREMENTS OF LOW-LOSS DIELECTRICS

The theory behind measuring low-loss (i.e. THz transmission greater than  $\approx 97\%$ ) dielectrics with the resonator approach is outlined by Yu and Cullen [33]. A comparison of the resonance peaks measured in the unloaded case and the dielectric/low-loss semiconductor configuration shown in Fig. 3 allows extraction of the dielectric constant and loss tangent. The insertion of a low-loss dielectric sample changes the effective optical path

length of the resonator as well as the single-pass loss compared to the unloaded case.

The first step in measuring the relative permittivity is to obtain a good estimate of the unloaded resonator length,  $L$ , so that the exact mode number of the resonance can be determined. An initial estimation of  $L$  can be made by finding the center frequencies of multiple resonance peaks and relating the peak spacing,  $\Delta\nu$ , to the resonator length

$$\Delta\nu = \frac{c}{2L} \quad (15)$$

where  $c$  is the speed of light in the propagation medium. The resulting  $L$  can be further improved by using it as an initial guess to numerically solve a more accurate equation for the resonant frequency  $\nu_u$  [33]

$$\nu_u = \frac{c}{4L} \left[ q + 1 + \frac{1}{\pi} \arccos \left( 1 - \frac{2L}{R_m} \right) - \frac{1}{2\pi\beta_u R_m} \right] \quad (16)$$

where  $q$  is the mode number,  $R_m$  is the curvature radius of the spherical mirror, and  $\beta_u = 2\pi\nu_u/c$  is the wave number corresponding to the unloaded resonance frequency,  $\nu_u$ .

Once the measurement for the unloaded case is complete, the low-loss sample is attached to the flat mirror as shown in the low-loss dielectric/semiconductor configuration in Fig. 3. After recording the new peak frequencies and quality factors, the relative permittivity can be found by solving the transcendental [18]

$$\frac{1}{n} \tan(n\beta_L t - \Phi_T) = -\tan(\beta_L d - \Phi_D) \quad (17)$$

where

$$\begin{aligned} \Phi_D &= \arctan \left( \frac{d + \frac{t}{n}}{z_L} \right) - \arctan \left( \frac{1}{\beta_L R_m} \right) \\ &\quad - \arctan \left( \frac{t}{nz_L} \right) - \arctan \left( \frac{1}{\beta_L R_2(t)} \right) \\ \Phi_T &= \arctan \left( \frac{t}{nz_L} \right) - \arctan \left( \frac{1}{n\beta_L R_1(t)} \right) \end{aligned}$$

$$R_1(t) = t + \frac{n^2 z_L^2}{t}$$

$$R_2(t) = \frac{t}{n} + \frac{n z_L^2}{t}$$

and

- $d$  distance between sample and spherical mirror;
- $t$  thickness of sample;
- $n$  initial guess for sample refractive index;
- $\nu_L$  loaded resonance frequency;
- $\beta_L = 2\pi\nu_L/c$ ;
- $z_L = \sqrt{(d')(R_m - d')}$ ;
- $d' = d + (t/n)$ .

In order to solve the transcendental equation, an initial guess for the refractive index is necessary. For this purpose, a known value at the closest frequency possible is an adequate initial guess. In most cases the variation of the refractive index as a function of frequency is small enough to allow the numerical solver to arrive at the correct local solution.

TABLE I  
COMPARISON OF MEASURED VALUES OF RELATIVE PERMITTIVITY  
WITH VALUES FROM LITERATURE [3]

Sample Material	Measured Relative Permittivity ( $\epsilon_r$ )	Relative Permittivity in Literature ( $\epsilon_r$ ) [3]
Single-Crystal Quartz	$4.60 \pm 0.04$	4.64
Silicon	$11.89 \pm 0.02$	11.88

This approach has been used to successfully measure the relative permittivity ( $\epsilon_r = n^2$ ) for a silicon and quartz sample. Uncertainty in the sample thickness is the primary source of error in both cases. Table I summarizes the resulting measured values compared with those cited in [3].

The resonator can also be used to determine the loss tangent or conductivity of the low-loss sample. By measuring the quality factor of the unloaded resonator,  $Q_U$ , and the loaded resonator,  $Q_L$ , the effective quality factor due to the additional losses from the dielectric  $Q_\epsilon$  can be calculated

$$\frac{1}{Q_\epsilon} = \frac{1}{Q_L} - \frac{1}{Q_U}. \quad (18)$$

By correlating  $Q_\epsilon$  to the fractional loss-per-pass we can calculate loss tangent of the sample [33]

$$\tan \delta = \frac{2n\beta_L(d + t\Delta)}{Q_\epsilon [2n\beta_L t\Delta - \Delta \sin(2n\beta_L t - 2\Phi_T)]} \quad (19)$$

where

$$\Delta = \frac{n^2}{n^2 \cos^2(n\beta_L t - \Phi_T) + \sin^2(n\beta_L t - \Phi_T)}. \quad (20)$$

The conductivity,  $\sigma$ , of the sample relates to the loss tangent  $\tan \delta$  by

$$\sigma = 2\pi\nu_L n^2 \epsilon_0 \tan \delta. \quad (21)$$

The resonator has also been used to measure silicon samples of different doping densities for comparison with a self-consistent ensemble Monte Carlo/finite-difference time-domain (EMC/FDTD) simulation tool [34]–[36]. The EMC/FDTD tool has been benchmarked with past TDS measurements of silicon wafers [37]. The results are also compared with predictions from the Drude model, which describes the behavior of conductors and semiconductors at lower frequencies [38]

$$\sigma(\nu) = \frac{\sigma_{DC}}{1 + j2\pi\nu\tau} \quad (22)$$

where  $\sigma_{DC}$  is the conductivity for the dc case,  $\sigma(\nu)$  is the frequency-dependent conductivity, and  $\tau$  is the characteristic scattering time. The results of these measurements are shown in Figs. 6 and 7.

The EMC/FDTD results show a closer match to the measured values than the predictions by the Drude model, especially at higher doping densities. The increasing deviation between the EMC/FDTD simulation and the Drude model at higher doping densities further motivates developing the EMC/FDTD

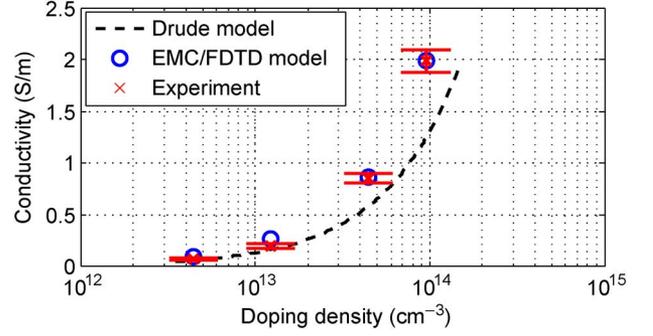


Fig. 6. Measured conductivity values compared with EMC/FDTD simulation results and Drude model predictions at 400 GHz.

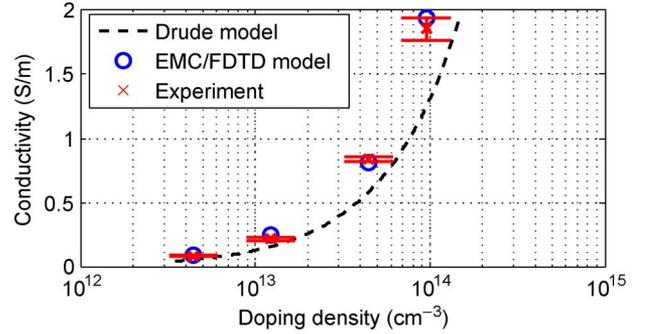


Fig. 7. Measured conductivity values compared with EMC/FDTD simulation results and Drude model predictions at 650 GHz.

approach as the physics model of choice for high-conductivity materials in the THz regime.

#### IV. MEASUREMENTS OF GOOD CONDUCTORS

Another primary application of the resonator is to measure the THz conductivity of metals with sub-micron roughness features. The effective THz conductivity of a planar, metallic sample can be found by substituting it in place of the reference copper mirror as shown in the metals configuration in Fig. 3. The change in quality factor when compared to the unloaded case of Fig. 3 directly correlates to the difference in reflection losses of the substituted flat copper mirror. Since all other sources of loss are characterized, the reflection loss of the sample, and thus the effective conductivity, can be extracted.

As described in Section II-B, the atmospheric ( $\kappa_A$ ), diffraction ( $\kappa_D$ ), and alignment ( $\kappa_L$ ) losses have been made negligible compared to the remaining sources of loss in Fig. 2. The measured quality factor,  $Q_{tot}$ , of the resonator can therefore be approximated by (9), repeated here for convenience:

$$\frac{1}{Q_{tot}} = \frac{c}{2\pi\nu_c L} \left[ \kappa_C + \frac{1}{2}(\kappa_{R1} + \kappa_{R2}) \right]$$

where  $\nu_c$  is the resonant frequency and  $L$  is the resonator length that can be found by using (15) as a starting point.  $\kappa_C$  is the coupling loss, which is a known quantity from the cavity characterization performed in Section II-B.  $\kappa_{R1}$  and  $\kappa_{R2}$  represent the reflection losses in the spherical and planar mirror, respectively. The cavity characterization of Section II-B also provided the value for the resistive loss of the spherical mirror ( $\kappa_{R1} = \kappa_R^{Cu}$ ).

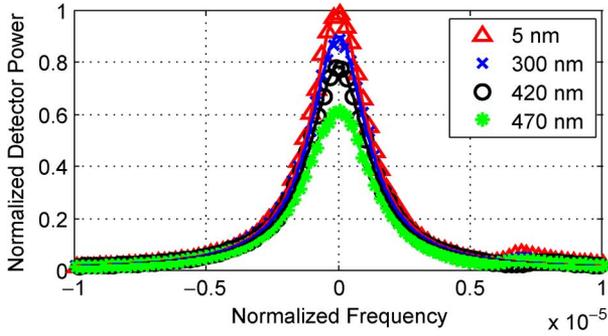


Fig. 8. Normalized measured peaks for different lapped copper planar mirror samples.

By replacing the flat mirror with a planar sample of unknown conductivity and resistive loss ( $\kappa_{R2} = \kappa_R^S$ ) (9) becomes:

$$\frac{1}{Q_{\text{tot}}} = \frac{c}{2\pi\nu_c L} \left[ \kappa_C + \frac{1}{2} (\kappa_R^{\text{Cu}} + \kappa_R^S) \right]. \quad (23)$$

Solving (23) reveals the value of  $\kappa_R^S$

$$\kappa_R^S = 2 \left[ \frac{2\pi\nu_c L}{Q_{\text{tot}} c} - \kappa_C \right] - \kappa_R^{\text{Cu}}. \quad (24)$$

Once the effective loss of the sample,  $\kappa_R^S$ , is found, the effective conductivity,  $\sigma_S$ , of the sample can be calculated with the following [6]

$$\sigma_S = \frac{16\pi\nu_c \epsilon}{(\kappa_R^S)^2}. \quad (25)$$

Depending on the resonator length after sample insertion, there are three to four resonance peaks in the usable 4 GHz bandwidth of the AMCs. To ensure repeatability, each peak was measured three times for each sample for a total of nine to twelve scans at a resolution of  $\Delta\nu = 0.144$  MHz. Choice of the frequency resolution is important for accuracy. A resolution that is too fine can result in data sampling over too long a time frame and degrade measurement accuracy due to drifting conditions such as temperature fluctuations. If the resolution is too coarse, then the accuracy of the Lorentzian curve fit and the extraction of the quality factor is potentially compromised. Through trial-and-error, an optimal frequency step size that provided consistent curve fit results while performing the scan as quickly as possible was found.

The resonator was used to measure the effective THz conductivity at 650 GHz of copper samples that were machined to different root mean square (RMS) roughness values. Fig. 8 shows typical normalized resonance peak measurements of the resonator with different samples acting as the planar mirror. The legend shows the planar mirror RMS roughness values. As expected, the maximum power decreases and the peak broadens with increased roughness in the planar mirror.

Fig. 9 shows the effective surface resistance extracted from repeated measurements of multiple peaks that were curve-fitted to the Lorentzian using the techniques described in Section II-B. The experimental results are compared with a model by Saillard and Maystre for rough surface scattering [39]. Using an integral

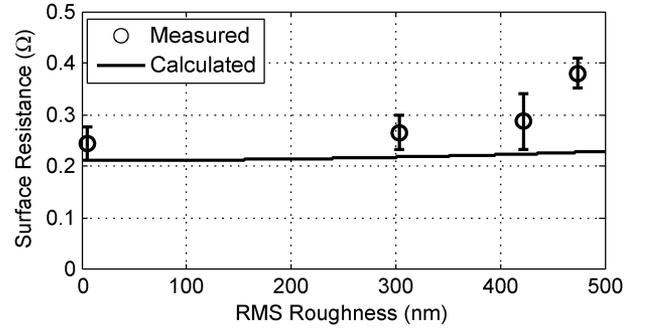


Fig. 9. Measured surface resistance of different lapped samples with different average roughness features.

theory approach, they derived a relationship between the RMS roughness of a metal surface,  $\xi$ , and the reflectivity,  $R_{mi}^r$ , for normal incidence:

$$R_{mi}^r = R_{mi}^s e^{(-4\pi\nu\xi/c)^2}. \quad (26)$$

The smooth-surface reflectivity,  $R_{mi}^s$ , can be directly calculated using the predicted surface resistance values of the classical relaxation-effect model [4], which should be valid at this frequency [7]. The surface impedance,  $Z_S$ , can be written as

$$Z_S = \sqrt{\frac{j\omega\mu}{\sigma_R + j\omega\epsilon}} \quad (27)$$

$$\sigma_R = \frac{\sigma_{DC}}{1 + j\omega\tau}$$

where  $\omega$  is the frequency in radians per second,  $\sigma_{DC}$  is the bulk direct current (DC) conductivity of copper, and  $\tau$  is the known carrier scattering rate of the metal [4].

The measurements show a reasonable agreement for a smooth surface. As the roughness increases, however, the surface resistance increases more sharply than the model predictions. While the model has been verified at 120–140 GHz [40], the deviations at 650 GHz suggest that further exploration of roughness effects on THz conductivity is warranted at higher frequencies.

## V. CONCLUSION

The quasi-optical resonator system in this paper pushes the frequency boundaries of a resonator approach to measuring dielectric and conductor properties beyond 400 GHz. Several changes from lower frequency designs were necessary to obtain a sufficiently high quality factor for sensitive measurements of effective conductivity, such as the combination of the AMC and Golay cell with a lock-in amplifier, the implementation of the single coupling film with wire grids, and reformulation to incorporate non-negligible coupling film loss. The resulting apparatus can measure effective conductivity with an accuracy of 10% or better.

While the apparatus in this paper demonstrates operating frequencies of 400 and 650 GHz, the principles of the technique can be implemented beyond 1 THz. The primary limitation is the availability of an adequately powerful radiation source and a sufficiently sensitive detector to overcome the  $\approx 10^4$  insertion loss. This loss can be decreased through the use of thicker coupling films, though it is at the expense of the quality factor and measurement sensitivity.

The resonator was used to measure silicon with doping densities between  $10^{12}$  and  $10^{14}$   $\text{cm}^{-3}$  with good agreement to a benchmarked EMC/FDTD model. A disagreement with the Drude model was found with increased doping density, establishing the EMC/FDTD approach as the model of choice in the THz regime.

Measurements of copper surfaces with sub-micron surface roughness values were performed at 650 GHz and compared with theory. While a good agreement was found for smoother surfaces, the theory was a poor predictor of surface conductivity with increased roughness. The reason for this discrepancy is not well understood at this time and is the subject of future study.

The results in this paper not only indicate a need for further characterization of the effects of surface roughness on conductivity in the THz regime but also demonstrates that the resonator in this paper is a capable instrument for such studies. The small measurement region of this setup makes it the ideal tool to examine samples with nanofabricated textures using techniques such as electron beam lithography that become very expensive when patterning over large areas.

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